

# Pinned Frames

- 2-Force Members
- Multiforce Members
- Stability
- Timber Frames

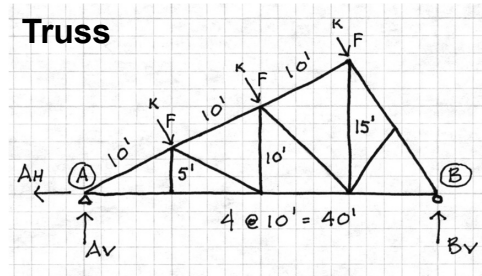


Das Spitzhäuschen. Marktplatz. Bernkastel-Kues

## Pinned Frame vs. Truss

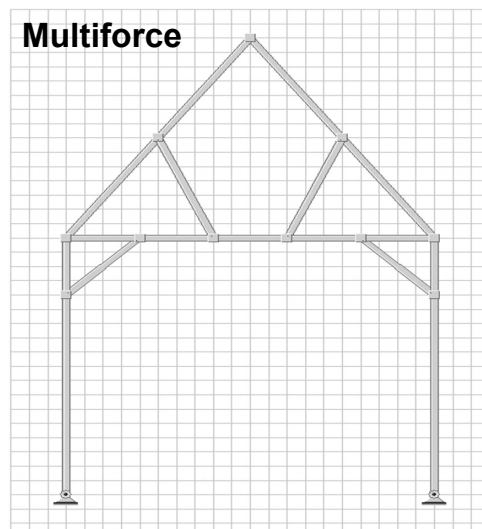
Trusses:

- 2-force members
- ridged bodies

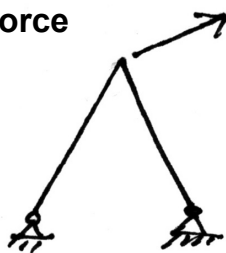


Pinned Frames:

- 2-force or multiforce (axial or bending)
- ridged body or mechanism

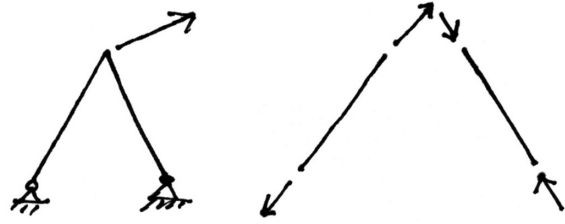


2-force

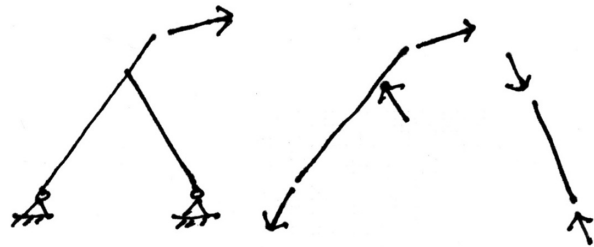


# Frame Types

Frames with 2-force members  
(axial forces)



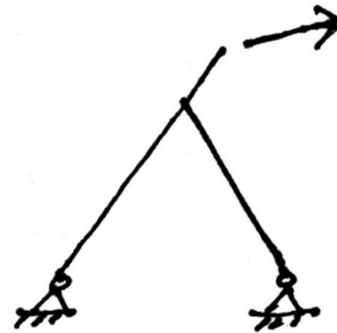
Frames with multiforce members  
(bending + axial forces)



# Rigidity

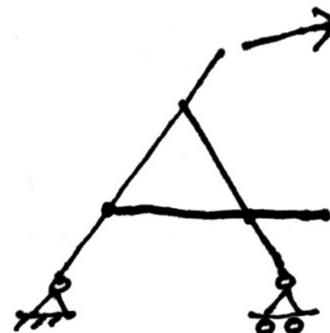
**Nonrigid frames** (require 4 or more  
reaction components for stability)

Without supports they collapse.



**Rigid frames** (only require 3 reaction  
components)

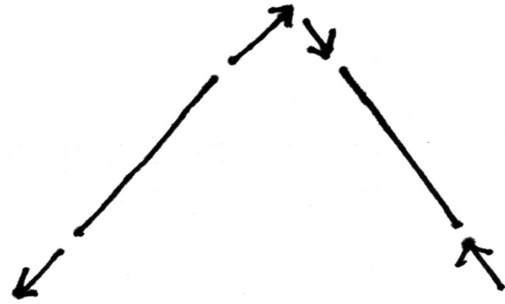
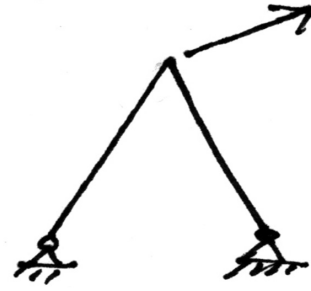
Remain a rigid body even without  
supports.



## 2-Force Member Frames

### Procedure

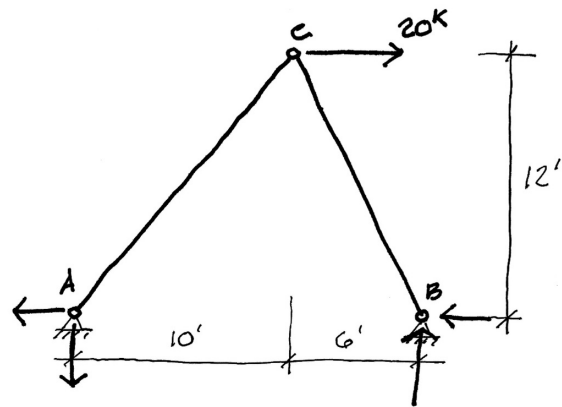
1. Solve external supports
  - FBDs
  - Simultaneous equations
2. Cut FBD of each member
3. Solve member forces



## 2-Force Member Frames

### Analysis

1. Solve external supports
  - FBDs
  - Simultaneous equations



$$\sum M @ A = 0 = 20(12) - B_v(16)$$
$$B_v = 15^k$$

$$\sum F_v = 0 = -A_v + B_v$$
$$A_v = 15$$

# 2-Force Member Frames

## Analysis

2. Cut FBD of each member

For 2-force members the force components follow the slope.

BY SLOPE

$$\frac{6}{5} : \frac{15}{12.5}$$

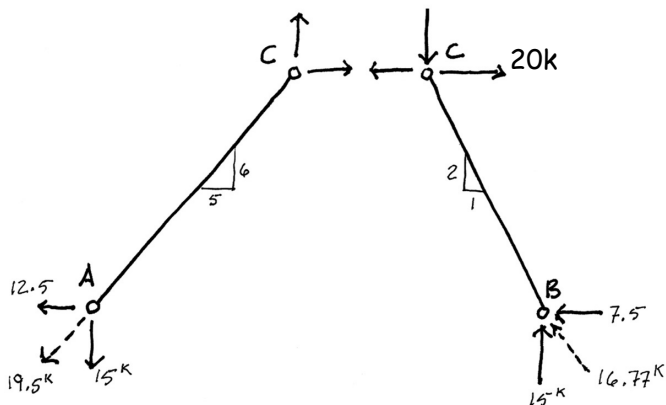
BY SLOPE

$$\frac{2}{1} : \frac{15}{7.5}$$

REACTION COMPONENTS

$$B_V = 15\text{K} \uparrow$$

$$B_H = 7.5 \leftarrow$$



# 2-Force Member Frames

## Analysis

3. Check member forces and balance forces.

LEFT FBD

$$\sum F_V = 0 = -15 + C_V$$

$$C_V = 15\text{K}$$

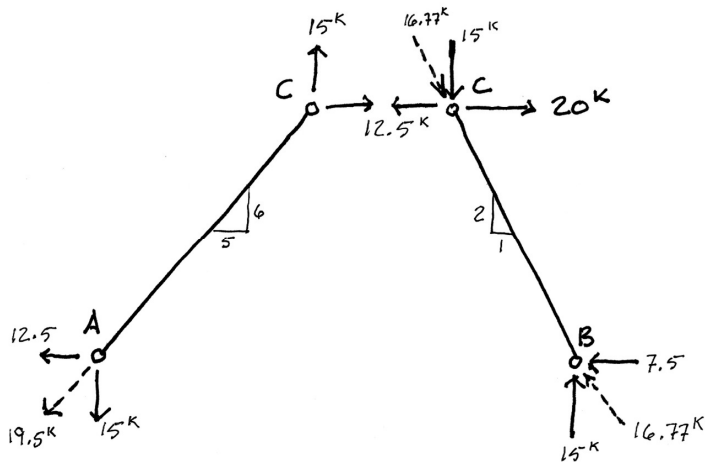
RIGHT FBD

$$\sum F_V = 0 = 15\text{K} - C_V$$

$$C_V = 15\text{K}$$

$$\sum F_H = 0 = 20\text{K} - 7.5 - C_H$$

$$C_H = 12.5\text{K}$$



## 2-Force Member Frames

Find the force in the shear legs assuming a point load of 20 **lbs**.  
Members **2:1 slope** (63.4° at base)

Determine the horizontal and vertical end reactions.

Reactions:

Horizontal \_\_\_\_\_

Vertical \_\_\_\_\_

Axial member force:

\_\_\_\_\_

tension or compression?

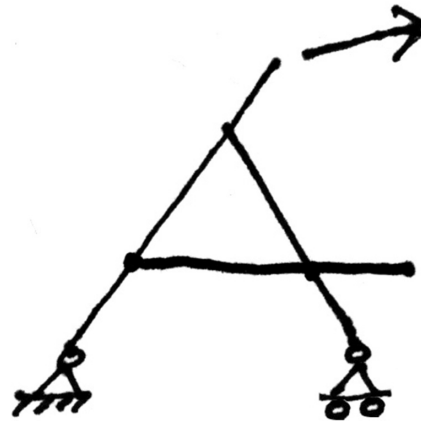
\_\_\_\_\_



## Multiforce Member Frames

Procedure

1. Solve external supports
2. Cut FBD of each member
3. Solve forces at joints.
4. Some members will be multiforce, they will be in bending.



# Analysis

## 1. Solve external supports

Get vertical components by summing moments.

$$\sum M_{@A} = 0$$

$$20^k(12') + 15^k(20') - B_v(20') = 0$$

$$B_v = \underline{27^k \uparrow}$$

$$\sum F_v = 0$$

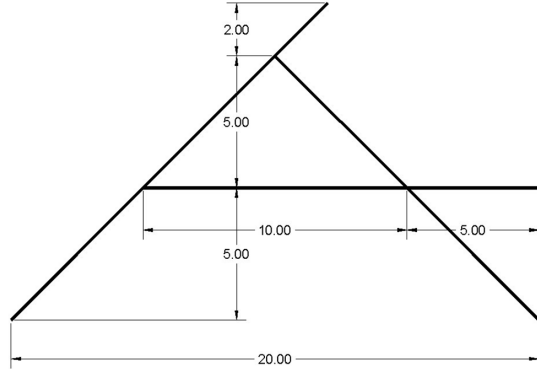
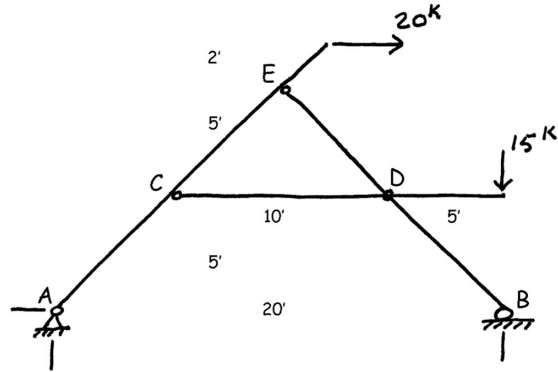
$$-A_v - 15^k + 27^k = 0$$

$$A_v = \underline{12^k \downarrow}$$

$$\sum F_H = 0$$

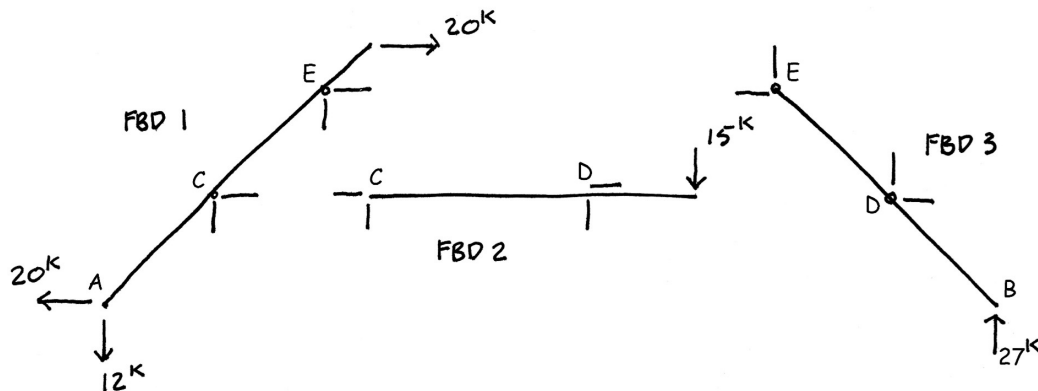
$$-A_H + 20^k = 0$$

$$A_H = \underline{20^k \leftarrow}$$



# Analysis

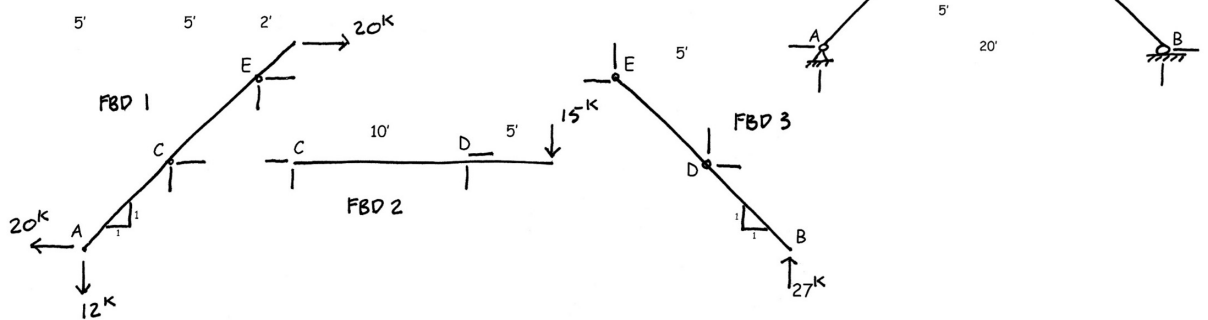
## 2. Cut FBD of each member



- Work between the FBDs using 3 equations of statics.
- End force components can be solved as axial and normal forces.
- The normal forces are “shear” forces and result in moments or “bending” forces.
- Not all systems are statically determinate and may then require other methods.

# Analysis

3. Solve member forces



FBD 2

$$\sum M_{@D} = 0 = -C_v(10') + 15^k(5')$$

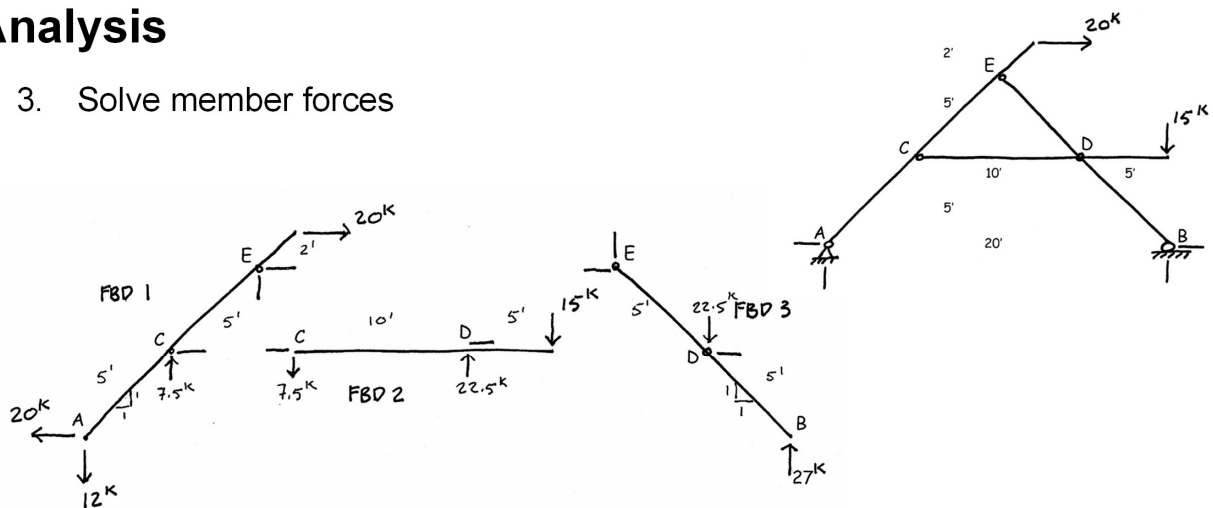
$$C_v = 7.5^k$$

$$\sum F_v = 0 = -7.5^k + D_v - 15^k$$

$$D_v = 22.5^k$$

# Analysis

3. Solve member forces



FBD 1

$$\sum M_{@E} = 20^k(10') - 12^k(10') + 7.5^k(5') - C_H(5') + 20^k(2') = 0$$

$$200 - 120 + 37.5 - C_H(5) + 40 = 0$$

$$C_H = 31.5^k$$

$$\sum F_v = 0 = -12^k + 7.5^k + E_v$$

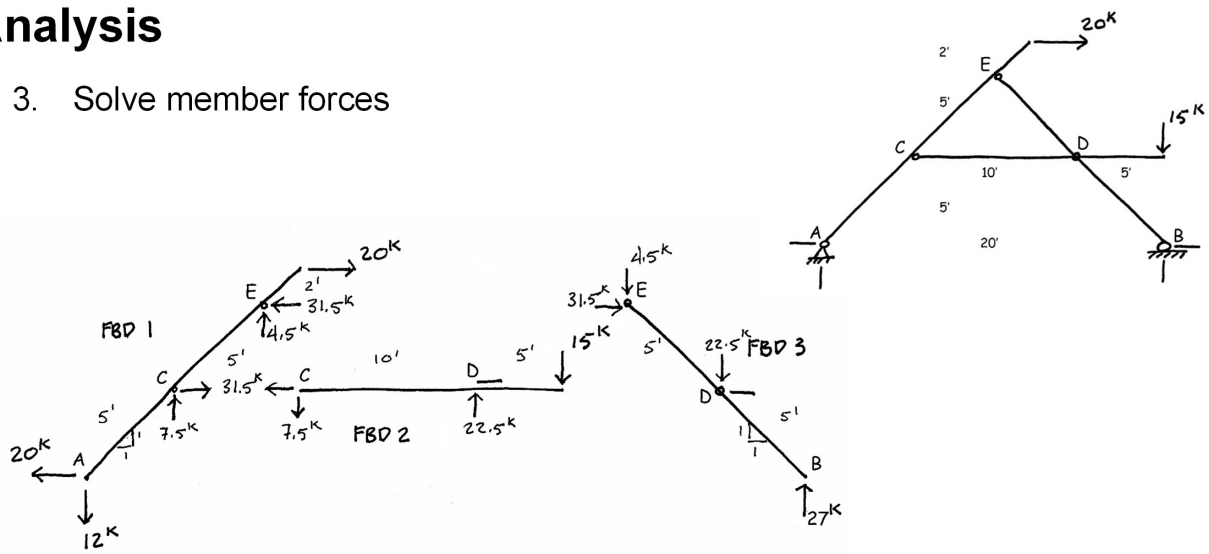
$$E_v = 4.5^k$$

$$\sum F_H = 0 = -20^k + 31.5^k - E_H + 20^k$$

$$E_H = 31.5^k$$

# Analysis

3. Solve member forces



FBD 2

$$\sum F_H = 0 = -31.5^k + D_H$$

$$D_H = 31.5^k$$

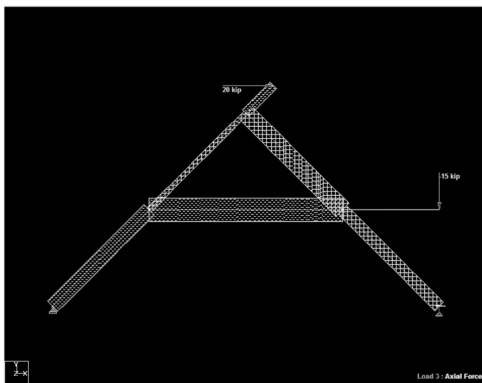
FBD 3 - CHECK

$$\sum F_H = 31.5^k - 31.5^k = 0 \quad \checkmark$$

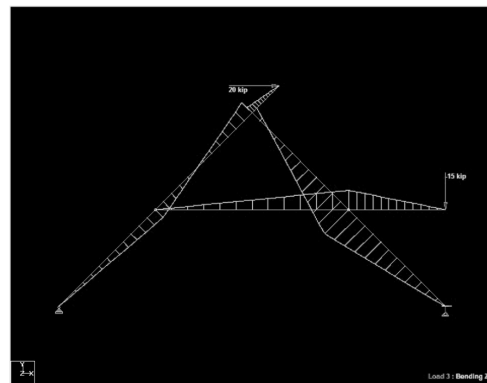
$$\sum F_V = -4.5^k - 22.5^k + 27^k = 0 \quad \checkmark$$

# Analysis

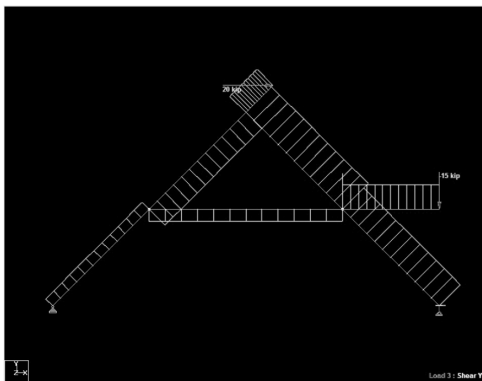
4. Determine multforce members



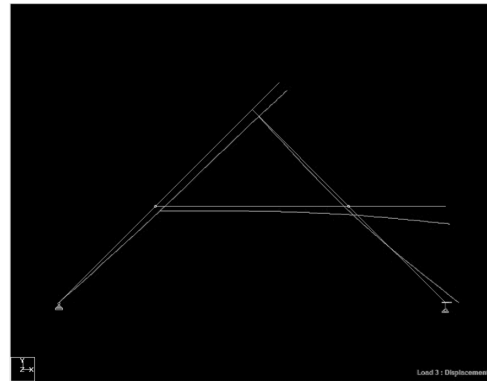
Axial Force



Bending Moment



Shear Force



Deflection



# Riverbend Timber Framing

<https://www.riverbendtf.com/>



**Marty Birkenkamp**



University of Michigan, TCAUP

Structures I

Slide 17 of 21

# Pariseau Barn

## Example



University of Michigan, TCAUP

Structures I

Slide 18 of 21

# Pariseau Barn Example



Motise and Tenon Joint



# Highland Timber Framing - <https://www.highlandtimberframing.com/>





## Our Stock Pavilion Series

Are you looking for a backyard pavilion that will be beautiful and long-lasting? That won't look run down like the pavilions that big box stores sell? We now offer various timber frame pavilions in several stock sizes! All stock pavilions are offered in 4-post or 6-post configurations. We're happy to create one in your preferred size.

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#### Queen Post Purlin Pavilions

Commonly used historically in covered bridges, this truss boasts greater spanning capabilities than its brother the king post truss. Featuring two posts connecting the rafters to the tie beam, it combines functionality, strength, and simple elegance. The two posts create a focal point, perfect for a large window in a great room, or the chimney of a fireplace.



#### King Post Rafter Pavilions

This is the simplest of the Highland Pavilion frames, with a heightened focus on simplicity and strength. It is based on the American timber framing tradition and boasts fewer joints than its sister frame the Queen Post Rafter Style.



#### Vaulted Purlin Pavilions

This truss is a Highland original, echoing techniques used in England in the high middle ages. It features struts transferring load from the rafters down to the posts. The continuous struts create a vaulted soaring effect for the onlooker found often in chapels.



#### Queen Post Rafter Pavilions

Commonly used historically in covered bridges, this truss features more complexity, timber, and strength than its brother the king post (Rafter style) truss. This frame is based on the American timber framing tradition and echoes common lines seen in 17th-19th century barns.