

Load Tracing

Load Paths
Load Diagrams
Floor Systems



Gatti Wool Mill, Rome (Pier Luigi Nervi, 1951)

Load Combinations - ASCE-7

Load Types

- Dead Load - D
- Roof Live Load - L_r
- Floor Live Load - L
- Snow Load - S
- Wind Load - W
- Earthquake - E

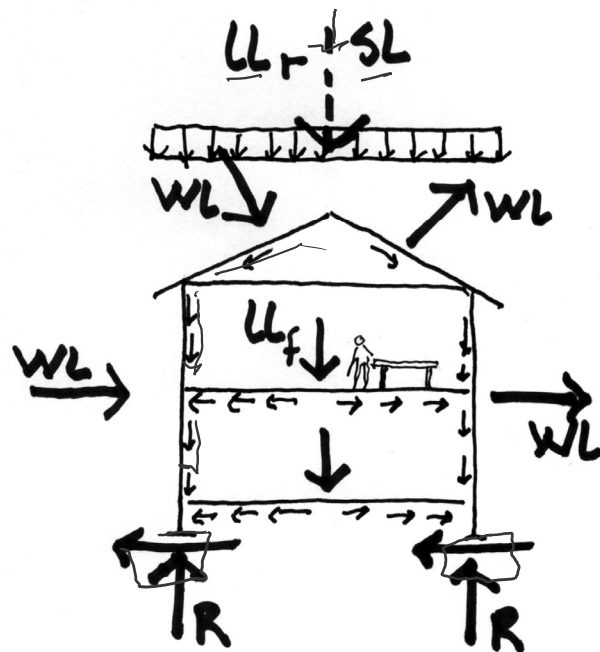
Load Combinations

Allowable Stress Design (ASD)

- D
- D + L
- D + (L_r or S)
- D + 0.75 L + 0.75 (L_r or S)
- D + (W or 0.7 E)

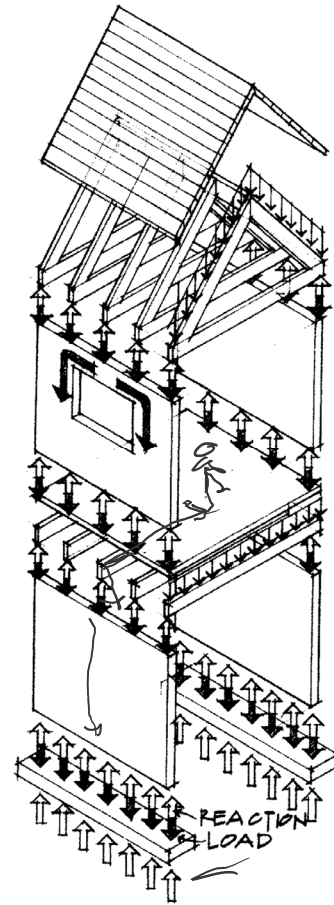
Load & Resistance Factored Design (LRFD)

- 1.4 D
- 1.2 D + 1.6 L_r + 0.5(L_r or S)
- 1.2 D + 1.6(L_r or S) + (L or 0.8W)
- 1.2 D + 1.6W + L + 0.5(L_r or S)
- 1.2 D + 1.6E + L + 0.2S



Load Paths

Gravity loads trace from top down to their resolution at the foundation.

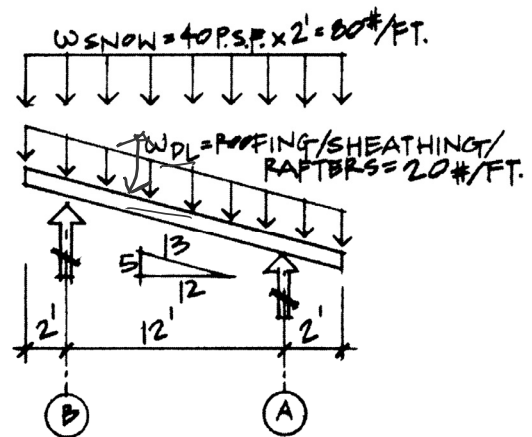


Load Paths

Roof Loads

Roof loads can be applied as **projected** loads (e.g., snow or live loads)

or loads on the surface (e.g., dead or wind)



Load Paths

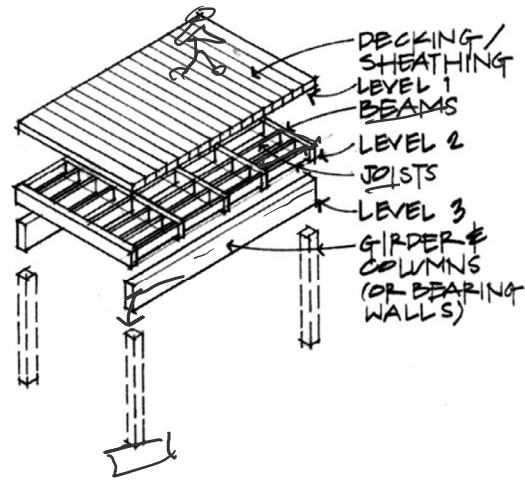
Floor Loads

Dead Load

weight of structure

Live Load

occupancy load



Member Hierarchy

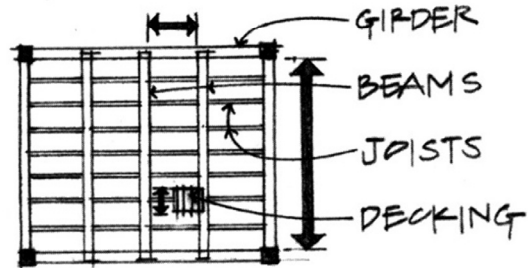
Flooring spans between joists

Joists span between beams

Beams span between girders

Girders span between columns

Columns carry load to ground



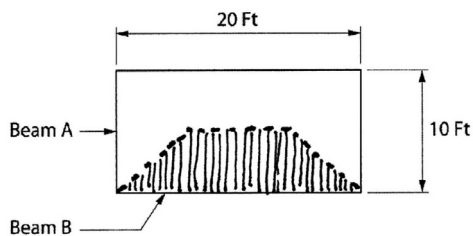
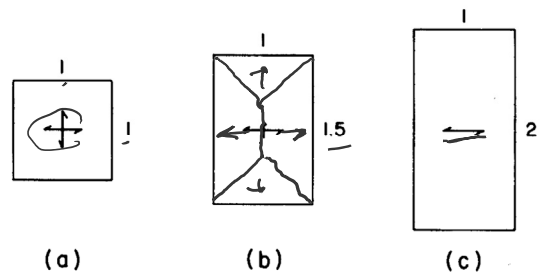
Load Paths

Floor Slabs

Concrete slabs span in the direction of the steel reinforcement.

One-way slabs should span the shortest direction.

Two-way slabs span in both directions. Aspect ratios should be square or less than 2:1. The load path divides at 45° from corner.



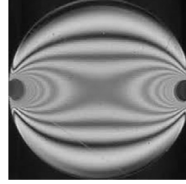
two-way slab tributary area of beam B



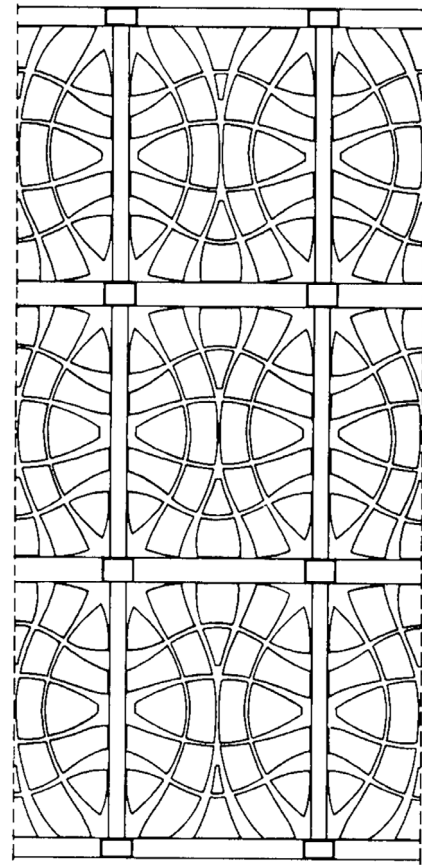
two-way waffle slab

Load Paths

Ideal load paths follow the **isoclines** of maximum tension and compression (principal stress patterns). These give the design with least material, but more complex form. They can be found using photoelastic models.



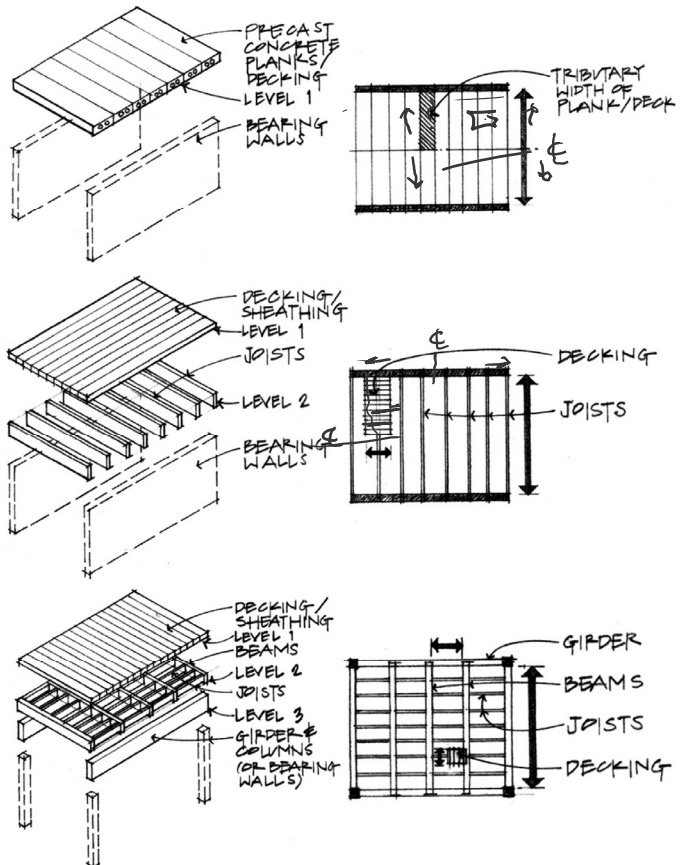
Cassa di Risparmio, Venice
by Pier Luigi Nervi



Tributary Area

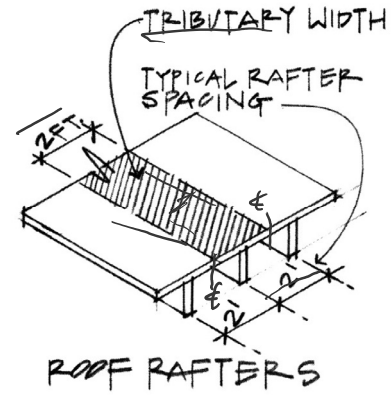
The **tributary area** is an area used to determine the load on a member.

If geometry and loading is symmetric, then load paths and reactions are also symmetric.

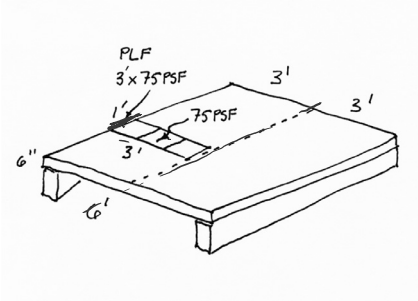


Tributary Area

The **tributary area** is an area used to determine the load on a member.



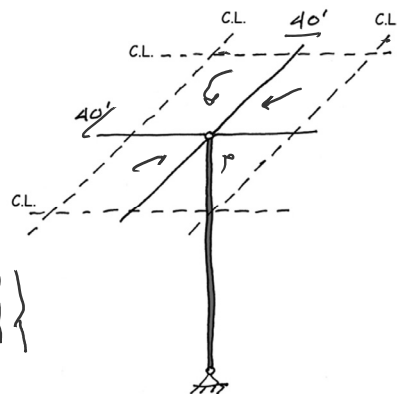
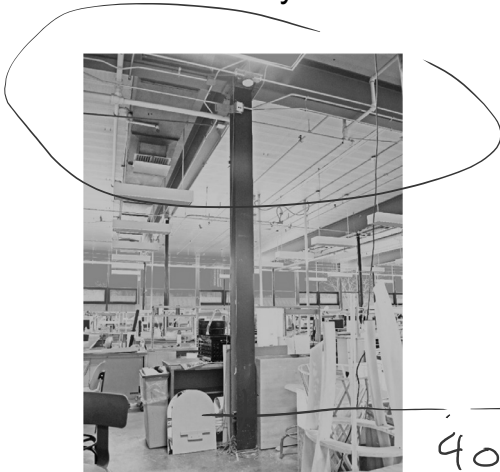
Each member has a tributary area that can be used to find the total load on that member.



Quiz

The columns on the third floor are set on a 40 foot grid.

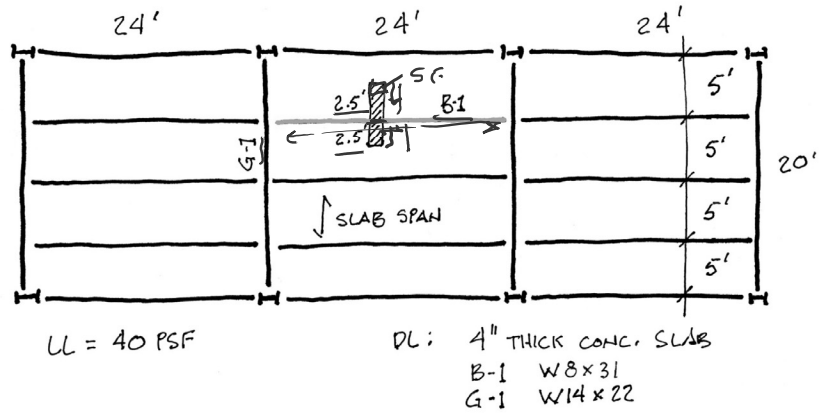
1. What is the tributary area of a central column? 5 K
2. For a roof $DL = 15 \text{ psf} + \text{roof } LL = 20 \text{ psf}$ how much load would the column carry?



Load Transfer

example 1

Construct the load diagram and find end reactions for **Beam B-1** and **Girder G-1**



For Load on B1:

Floor Dead Load = 4" slab + W8x31 beam

Floor Live Load = 40 PSF

DL slab = $150 \text{ PCF} \times (4/12) \text{ FT} = 50 \text{ PSE}$
 $50 \text{ PSF} \times (2.5' + 2.5') \text{ SF/LF} = 250 \text{ PLF}$

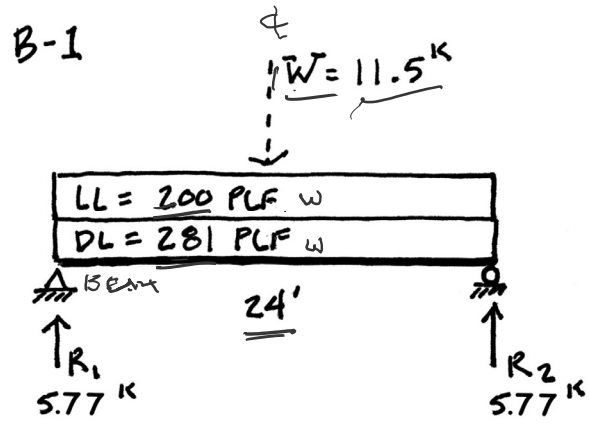
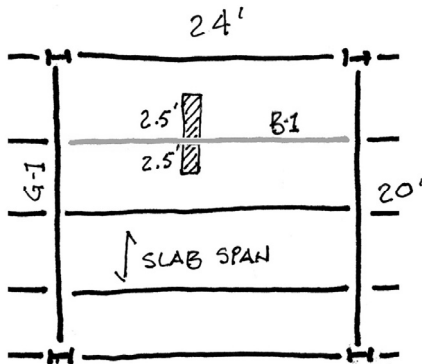
$40 \text{ PSF} \times (2.5' + 2.5') \text{ SF/LF} = 200 \text{ PLF}$

DL beam W8x31 (selfweight) = 31 PLF

TOTAL DL = $250 + 31 = 281 \text{ PLF}$

Load Transfer example 1

Construct load diagram and find end reactions for beam **B-1**

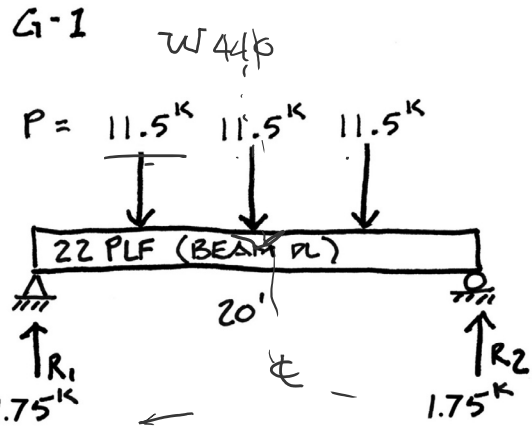
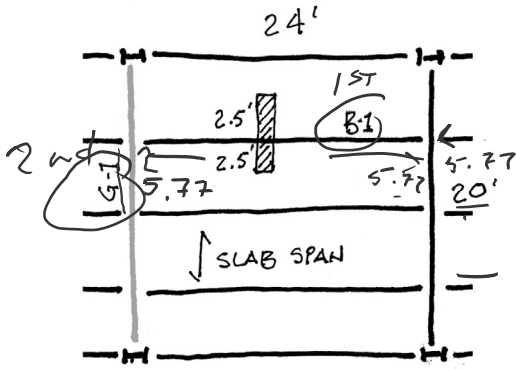


$W = wL = 481 \text{ PLF} \times 24' = 11544 \text{ LBS}$
 $R_1 = R_2 = 5772 \text{ LBS (BY SYMMETRY)}$

Load Transfer example 1

Construct load diagram and find end reactions for girder **G-1**

W14x22



$$\text{BEAM DL} = 22 \text{ PLF} \times 20' = 440 \text{ LBS}$$

$$P = 5772 \times 2 \text{ (from each side)} = 11544 \text{ LBS}$$

$$\text{TOTAL LOAD} = 3 \times 11544 + 440 = 35072 \text{ LBS}$$

$$R_1 = R_2 = 35072 / 2 = 17536 \text{ LBS}$$

Floor System

example 2

Find Load Diagrams for:

- B1
- B2
- G1

Dead Load

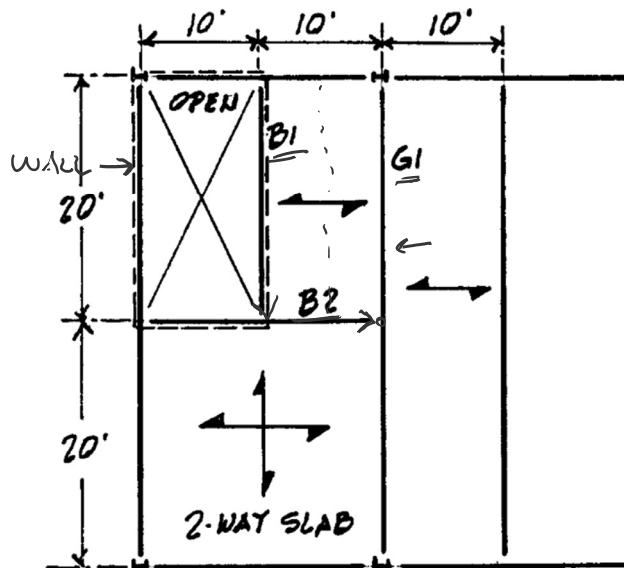
- wall 800 PLF
- floor slab 70 PSF

Live Load

- floor 90 PSF

Notice the order:

B1, then B2, then G1



Concrete slab floor system spanning in directions shown

Floor System example 2 cont.

Find a beam not loaded by other beams, e.g., a joist or a simple beam.

Sketch the tributary area – 1/2 span to the next member.

Sketch a load diagram

Calculate the distributed loads in PLF

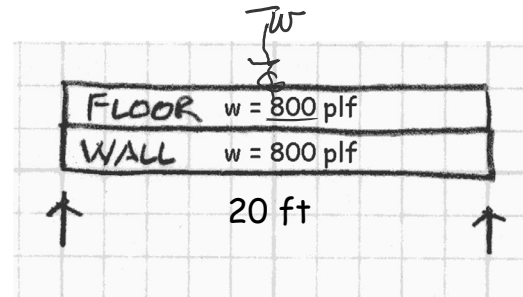
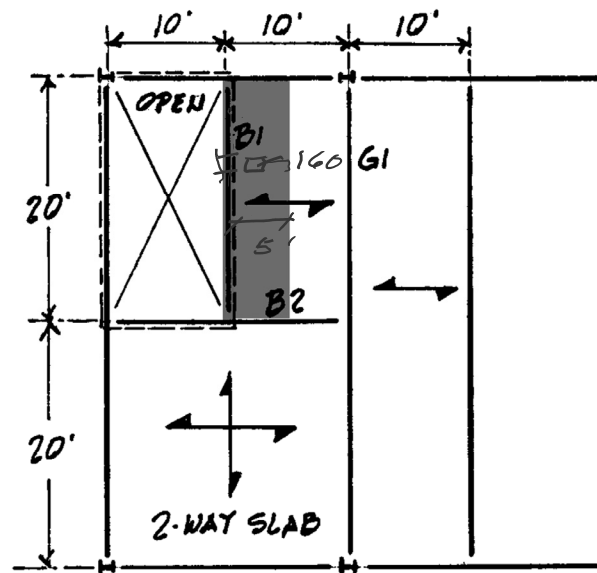
(total DL+LL on floor = 160 PSF)
 $70 \text{ PSF} + \underline{90 \text{ PSF}} = \underline{160 \text{ PSF}}$

Floor:

$$\underline{160 \text{ PSF}} \times \underline{5 \text{ FT}} = \underline{800 \text{ PLF}}$$

Wall:

$$800 \text{ PLF}$$



Load diagram

Floor System example 2 cont.

From the PLF loading, calculate a total W load.

Locate W at the centroid of the distributed loading.

Solve the end reactions by summing moments about reactions or by proportions.

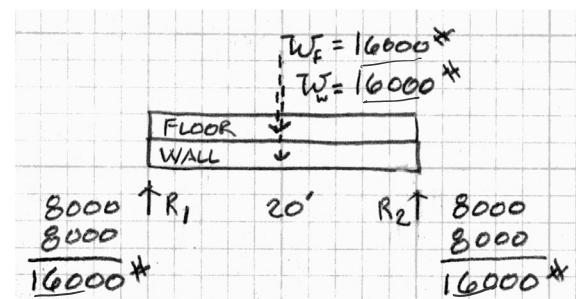
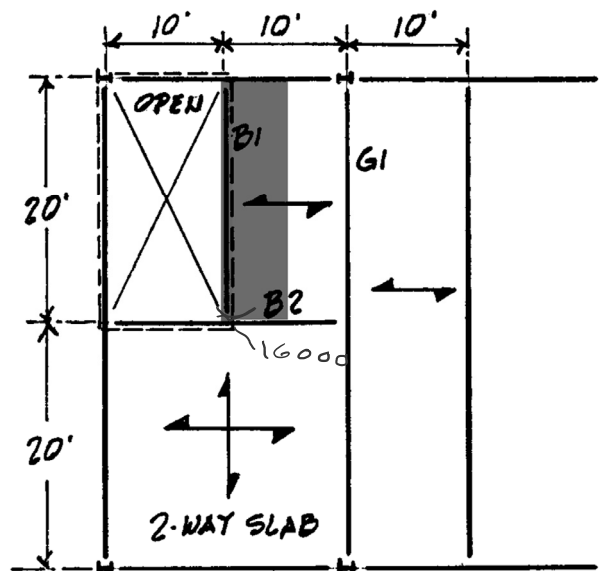
$$w \times L = W$$

Floor:

$$800 \text{ PLF} \times 20 \text{ FT} = 16000 \text{ LBS}$$

Wall:

$$800 \text{ PLF} \times 20 \text{ FT} = 16000 \text{ LBS}$$



Load diagram

Floor System example 2 cont.

Continue with the next beam supporting a previously solved beam.

Sketch the tributary areas – 2-way slabs divide at 45° from each corner. Areas associated with reactions of other beams are proportional to the load distribution.

Sketch a load diagram

Calculate the distributed loads in PLF, finding peak values of varying loads.

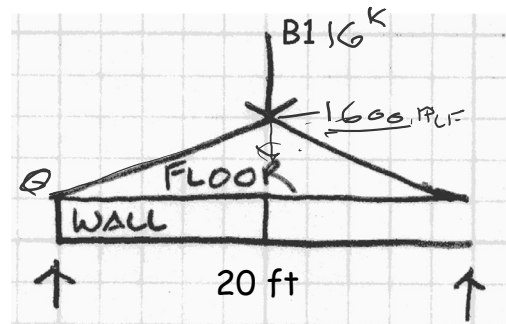
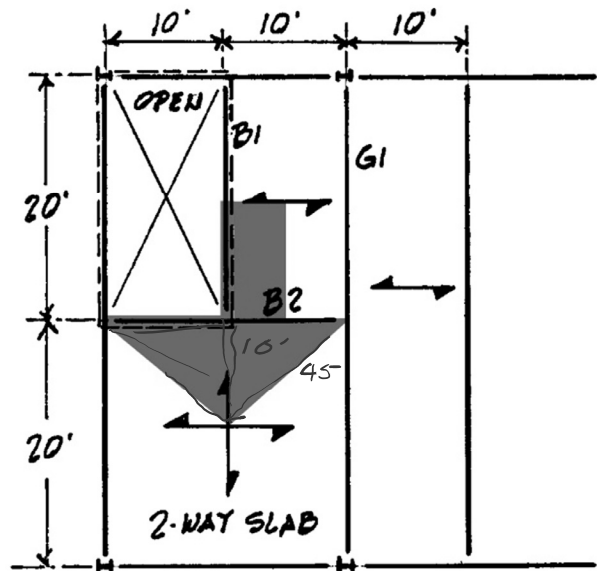
reaction from B1 = 16000 LBS

wall: DL = 800 PLF

floor: total DL+LL = 160 psf

2-way Slab (Peak Load)

$160 \text{ PSF} \times 10 \text{ FT} = 1600 \text{ PLF}$



Load diagram

Floor System example 2 cont.

From the PLF loading, calculate a total W load.

Locate W at the centroid of the distributed loading.

Solve the end reactions by summing moments or by proportions.

Reaction from B1:

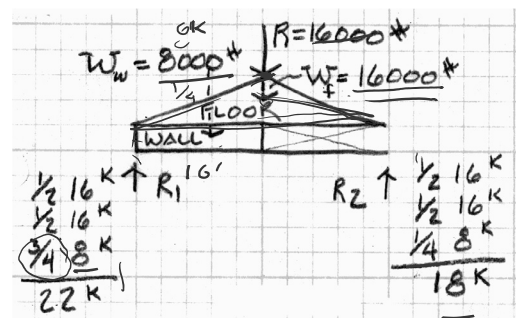
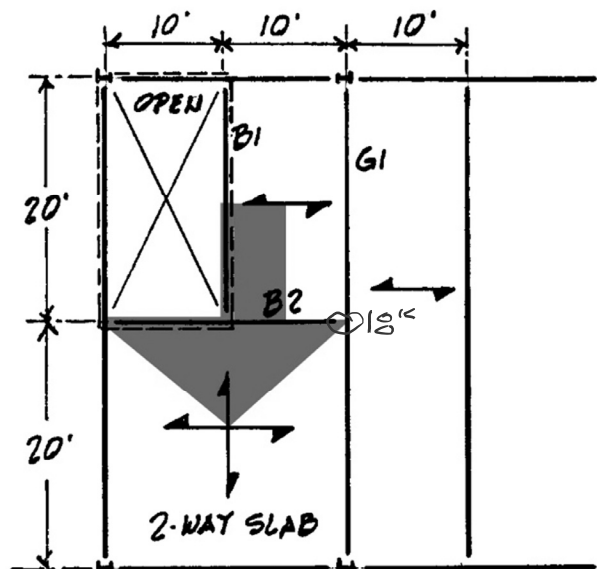
$R = 16000 \text{ LBS}$

Wall:

$800 \text{ PLF} \times 10 \text{ FT} = 8000 \text{ LBS}$

Floor:

$1600 \text{ PLF} \times 20 \text{ FT} / 2 = 16000 \text{ LBS}$



Load diagram

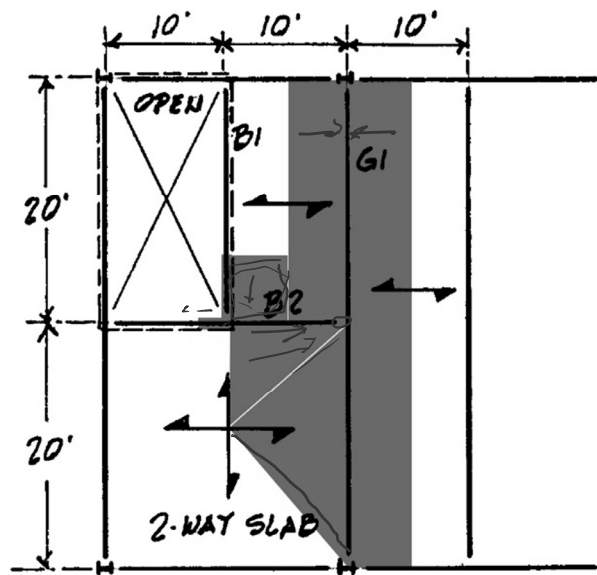
Floor System example 2 cont.

Continue with the next beam supporting a previously solved beam.

Sketch the tributary areas – 2-way slabs divide at 45° from each corner. Areas associated with reactions of other beams are proportional to the load distribution.

Sketch a load diagram

Calculate the distributed loads in PLF, finding peak values of varying loads.



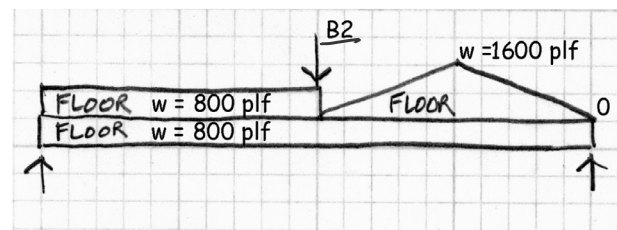
$$B2 = 18000 \text{ LBS}$$

Peak Load on 2-way Slab:

$$160 \text{ PSF} \times 10 \text{ FT} = 1600 \text{ PLF}$$

Floor on one side of G1:

$$160 \text{ PSF} \times 5 \text{ FT} = 800 \text{ PLF}$$



Load diagram

Floor System example 2 cont.

From the PLF loading, calculate a total W load.

Locate W at the centroid of the distributed loading.

Solve the end reactions by summing moments or by proportions.

reaction from B2:

$$18000 \text{ LBS}$$

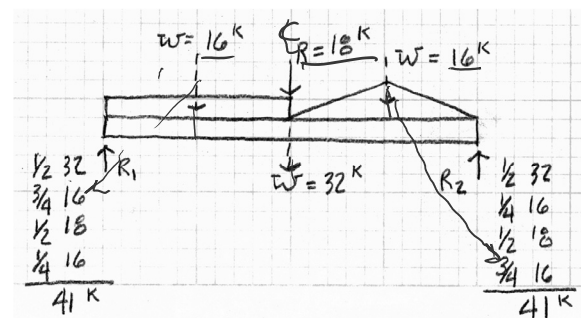
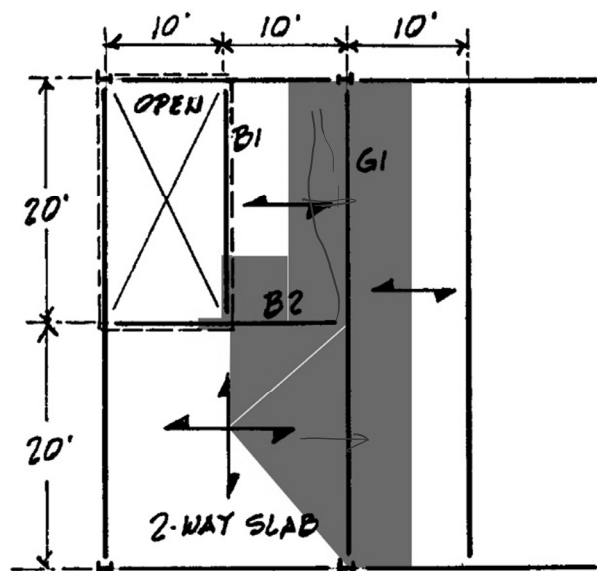
Floor on G1:

$$800 \text{ PLF} \times 20 \text{ FT} = 16000 \text{ LBS}$$

$$800 \text{ PLF} \times 40 \text{ FT} = 32000 \text{ LBS}$$

2-way Slab:

$$1600 \text{ PLF} \times 10 \text{ FT} = 16000 \text{ LBS}$$



Load diagram