#### ARCHITECTURE 314 STRUCTURES I

### Equilibrium Equations:

**Two-Dimensional** 

- Archimedes' Lever
- Newton's First Law
- Loading Types
- End Conditions
- Free Body Diagrams
- End Reactions



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Structures I

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# Archimedes of Syracuse (287 BC – 212 BC)

Greek mathematician, engineer, inventor

- The Lever (On the Equilibrium of Planes)
- The Screw (water pump)
- Greek Fire (to burn boats)
- Archimedes' Principle (density measure)
- Block and Tackle (for lifting on boats)
- Catapult
- Odometer
- Mathematical observations on circles and spheres







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## **Archimedes Lever**

Two forces will balance at distances reciprocally proportional to their magnitudes.



25

### **Archimedes Lever**

Two forces will balance at distances reciprocally proportional to their magnitudes.

Applied to beam end reactions:



1

41

2



## **Support Conditions**

### Roller

Fixed in Fy



### Free Body Diagrams

A Free Body Diagram (FBD) is a part cut from a larger force system.

When the FBD is cut free, all "exposed" forces are shown

If the complete system is in static equilibrium, then the FBD with forces at the cut will also be in equilibrium





### **End Reactions**

Example 1

- Given: Loads, Supports, Dimensions
- 1. Label components of reactions. Depending on the support condition, include vertical, horizontal and rotational.
- Convert <u>area loads</u> to <u>point</u> loads through the centroid 
  (balance point) of the area.
- Since there is only one horizontal force, it must equal zero.





### **End Reactions**

Example 1

- 4. Use the summation of moments about A to find  $R_B$ .
- 5. Use the summation of moments about B to find  $R_A$ .
- 6. Check calculation by summing vertical forces.



### End Reactions Example 3

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- Label components of reactions. You will need one equation for each unknown reaction.
- 2. Write an equation for the summation of moments.
- 3. Write an equation for the summation of vertical forces.
- 4. Write an equation for the summation of horizontal forces.
- 5. It is good practice to write one additional equation to check the results. In this case summation of moments at C also = 0.





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 \begin{array}{c} \Sigma F_{H} = 0 \\ 1 + 1 + 1 - H = 0 \\ H = 3 \\ \end{array}
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