

ARCH 314 STRUCTURE I

RECITATION SESSION 3
FACULTY: Prof. Peter Von Buelow
GSI: Faezeh Choobkar
FALL 2025

Welcome to recitation session

Introduction:

Faezeh Choobkar (PhD student)

Contact: faezehch@umich.edu

Office hours: by appointment

Outline:

Quick Recap

Provide the solution for the assignment (Problem set 3)

Answering student's questions

Recitation lab: Adding Forces

Problem Set 4 and 5

4. Parallel Force Systems

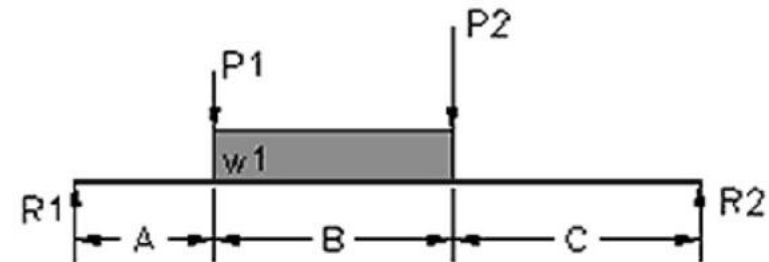
Sum the moments about each end of the beam to determine the end reactions of the parallel force system shown. Check that the sum of vertical forces is zero.

DATASET: 1

-2-

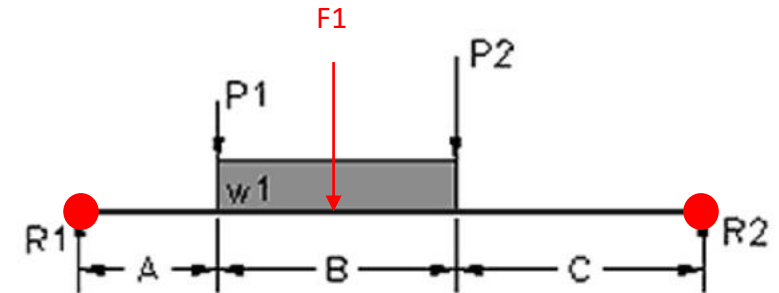
-3-

Distance A	6 FT
Distance B	12 FT
Distance C	4 FT
Force P1	5 KIPS
Force P2	1 KIPS
Force w1	0.9 KLF



Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	Total force from distributed load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance of total load W1 from left reaction	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	Total applied downward force	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Left End Reaction (R1)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
5	Right End Reaction (R2)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

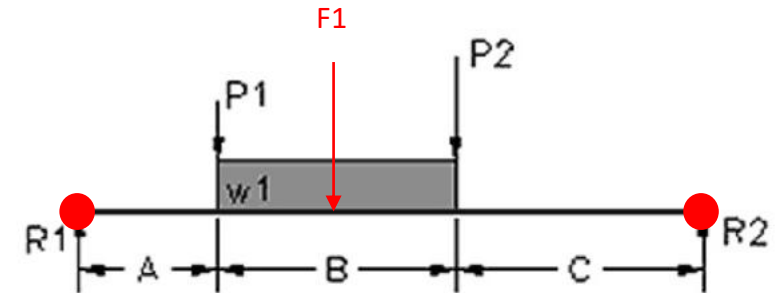


Q1:

$W1 = 0.9 \text{ KLF}$
 $\text{DISTANCE } B = 12 \text{ FT}$
 $\text{Total force} = F1 = 0.9 \times 12 = 10.8$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	Total force from distributed load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance of total load W1 from left reaction	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	Total applied downward force	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
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5	Right End Reaction (R2)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

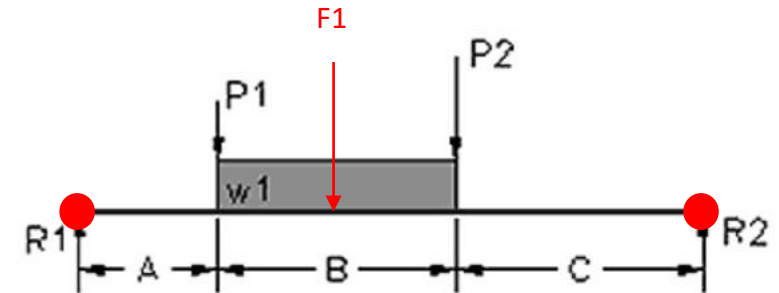


Q2:

Distance between F1 and R1:
Distance A + Distance B/2 = 12 FT

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	Total force from distributed load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance of total load W1 from left reaction	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	Total applied downward force	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Left End Reaction (R1)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
5	Right End Reaction (R2)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

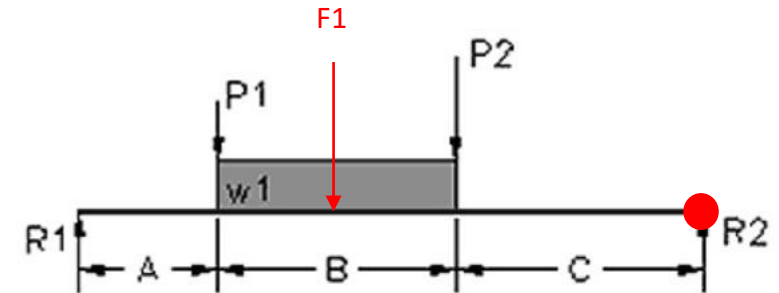


Q3:

Total downward force:
 $P1+P2+F1= 5+1+10.8= 16.8$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	Total force from distributed load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance of total load W1 from left reaction	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	Total applied downward force	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Left End Reaction (R1)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
5	Right End Reaction (R2)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>



Q4:

Left end reaction:

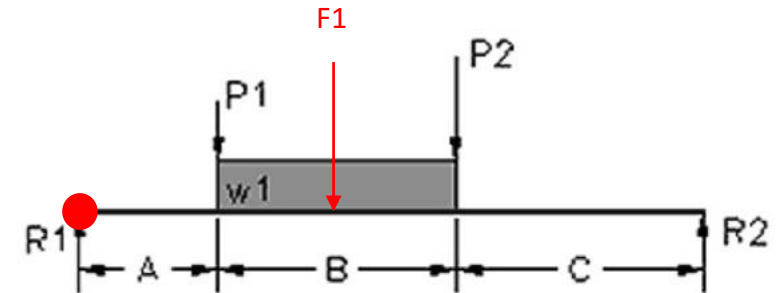
$$\sum M_2 = 0$$

$$R_1(6+12+4) - 5(12+4) - 1(4) - 10.8(10) = 0$$

$$R_1 = 8.73$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	Total force from distributed load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance of total load W1 from left reaction	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	Total applied downward force	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Left End Reaction (R1)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
5	Right End Reaction (R2)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>



Q5:

Right end reaction:

$$\sum M_1=0$$

$$-R_2(6+12+4)+5(6)+1(18)+10.8(12)=0$$

$$R_2=8.07$$

$$\sum F_y=0$$

$$8.07+8.73-16.8=0$$

Problem Set 4 and 5

5. Equilibrium of Rigid Bodies

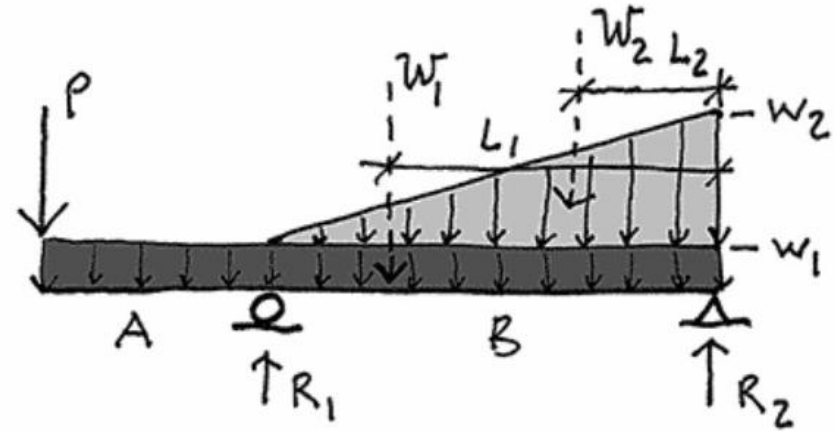
Determine the support reactions at A and B that will hold the beam in equilibrium.

DATASET: 1

-2-

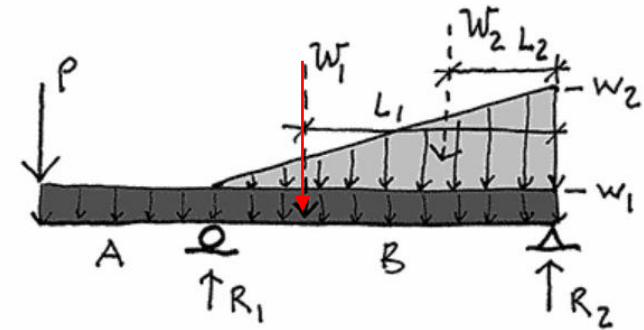
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Point Load: P	4.2 KIPS
Uniform Load: w_1	180 PLF
Triangular Load: w_2	520.8 PLF
Length A	6.3 FT
Length B	21 FT



Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
7	Reaction force: R2 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

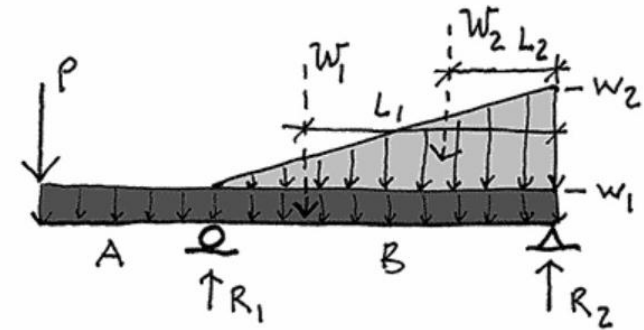


Q1:

$$W1 \times (A+B) = 180(27.3) = 4914 / 1000 = 4.914 \text{ KIPS}$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
7	Reaction force: R2 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

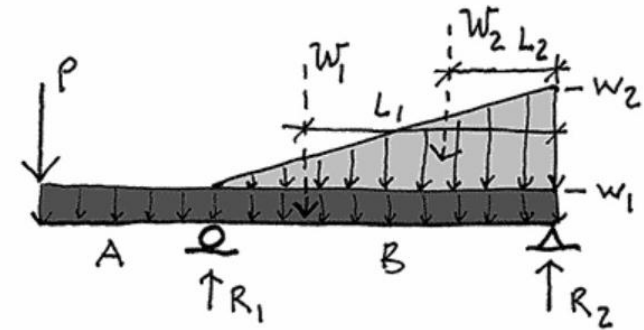


Q2:

$$L1 = (A+B)/2 = 27.3/2 = 13.65$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
7	Reaction force: R2 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

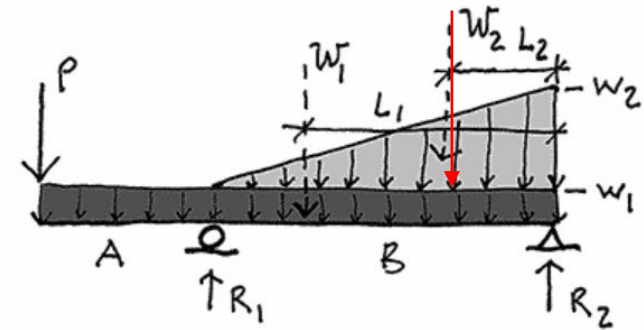


Q3:

$$520.8(B)/2=5468.4/1000=5.46$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
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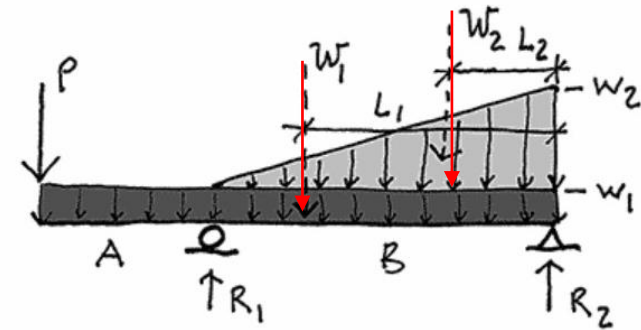


Q4:

$$\text{DISTANCE } B/3 = 21/3 = 7$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
7	Reaction force: R2 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>

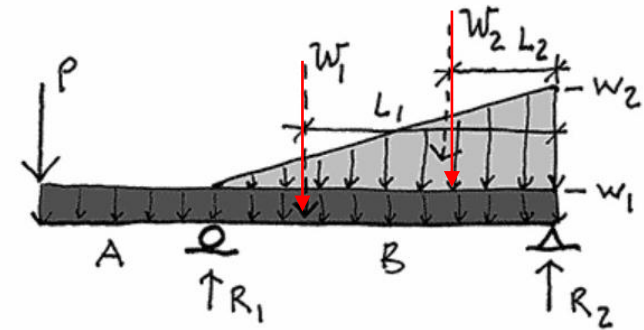


Q5:

$$\text{TOTAL LOAD} = P + W1 + W2 = 4.2 + 4.914 + 5.468 = 14.582$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
7	Reaction force: R2 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>



Q6:

Reaction R1:

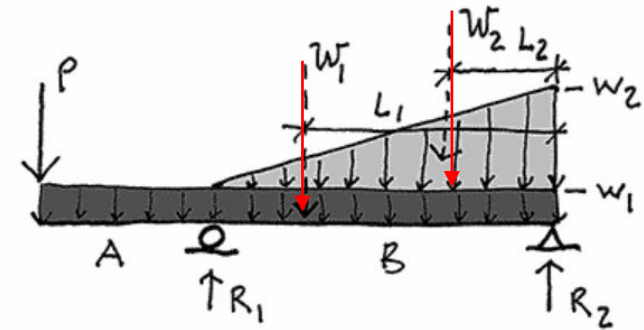
$$\sum M_2 = 0$$

$$-4.2(27.3) + R_1(21) - 4.914(13.65) - 5.46(7) = 0$$

$$R_2 = 10.47$$

Problem Set 4 and 5

#	Question	Your Response	Correct Answer
1	TOTAL force of the uniform load: W1	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
2	Distance from centroid of the uniform load to R2: (L1)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
3	TOTAL force of the triangular load: W2	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
4	Distance from centroid of the triangular load to R2: (L2)	<input type="text"/> FT	<input type="button" value="SUBMIT"/>
5	TOTAL load on the member	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
6	Reaction force: R1 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>
7	Reaction force: R2 (down is - : up is +)	<input type="text"/> KIPS	<input type="button" value="SUBMIT"/>



Q7:

Reaction R2:

$$\sum M_1 = 0$$

$$-4.2(6.3) + 4.914(7.35) + 5.46(14) - R_2(21) = 0$$

$$R_2 = 4.10$$

Equilibrium

LAB

Balance occurs when :
total clockwise moment = total counterclockwise moment

$$F_1 \cdot d_1 = F_2 \cdot d_2$$

$$\Sigma M = 0$$

$$\Sigma V = 0$$

Description

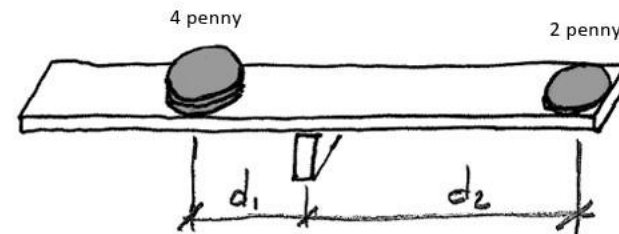
This project provides opportunity to experiment with the equilibrium of a balanced beam. It makes use of Archimedes' equations for forces on a lever to determine end reactions.

Goals

- To observe balanced conditions using a beam balance.
- To experiment with different combinations of balanced forces
- To calculate the balanced forces using Archimedes' method

Procedure

1. Set up the beam balance with the fulcrum block at the center balance point.
2. Place 2 penny weights at one end. Use the ruled scale at the bottom of this page to measure the distance from the fulcrum to the center of the stack of pennies (d_2). You can adjust the pennies to an even distance.
3. Calculate a point on the opposite side of the balance (d_1) where 4 pennies will balance the 2 using Archimedes' equation. $d_2 \times 2 = d_1 \times 4$ so, $d_1 = d_2 \times 2/4$
4. Place 4 pennies at your calculated distance d_1 and verify that they balance the 2 pennies.
5. Calculate the moment caused by each stack of pennies around the fulcrum (in US pennyweight-inches).
6. Now, leaving the 2 penny stack at one end, spread the 4 pennies out next to each other and again find the balance point.
7. Observe that the center of the line of pennies still lies at d_1 when the beam is balanced.
8. Finally, for the inverted case (point load on a simple beam) with $P = 6$ pwt at 2" from one end of the 12" beam, what would each end reaction be. Show this in a sketch.



Due

During recitation