

# Arch 314

# Structures I

Fall 2025 Recitation 004

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# Recitation 004

Welcome to session 6!

- Bridge!!
- Quick Recap of this week's lecture (+ part of last week's)
- Homework Review (#9 Floor Systems)
- Lab: Load Tracing

*Feel free to ask questions anytime*

# Bridge

## Due Dates:

- Bridge Testing - **11.03!!**
  - Sign up for testing slot if not already
- Final Report - 11.25 (right before Thanksgiving break)

## Key Rules:

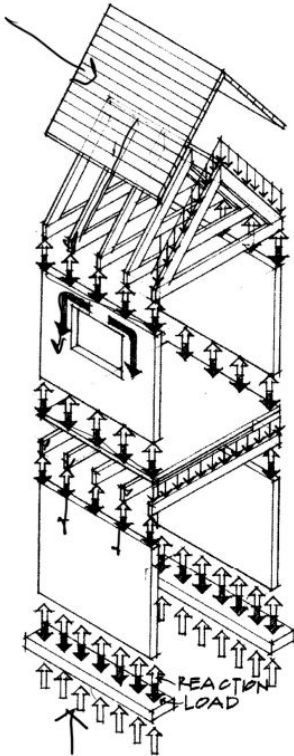
- Must load bricks on the deck
- Wood + Glue only
- MUST BE UNDER 4OZ
  - Scales will be down in Peter's office - do NOT remove them & make sure they are in oz not Toz
  - Note: for data gathering purposes - please weigh bridge materials before/without glue + again after glue

# Bridge

## Tips:

- See feedback on preliminary report
  - Don't forget lateral bracing
- Make sure you have lip on both ends to combat sagging and so the bridge can properly fit on stand (test downstairs!!)
- Account for 10% weight = glue
- Make a test bridge if possible
- DO NOT WAIT UNTIL THE LAST MINUTE
  
- Loading strategy - place on the joints and load fast! Have a system of who is holding/passing what (assembly line!)
  - Load across entirety of bridge - distribute load / not allowed to only load on ends

# Lecture: Load Tracing & Floor Systems (10/15)



## Load Paths

Floor Loads

### Dead Load

weight of structure

### Live Load

occupancy load

### Member Hierarchy

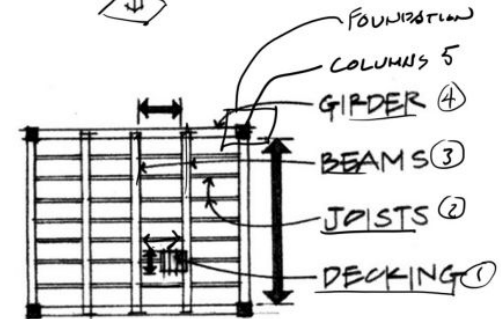
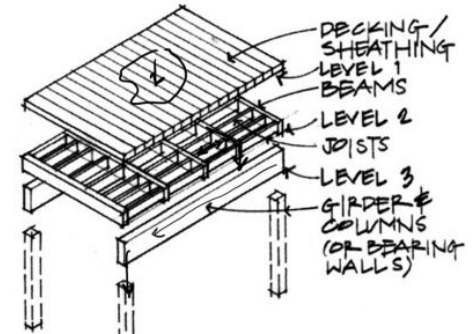
**Flooring** spans between joists

**Joists** span between beams

**Beams** span between girders

**Girders** span between columns

**Columns** carry load to ground



# Lecture: Load Tracing & Floor Systems (10/15)

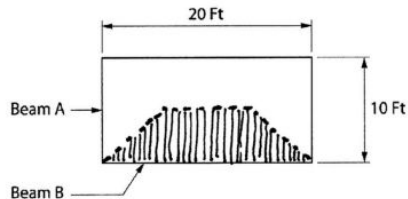
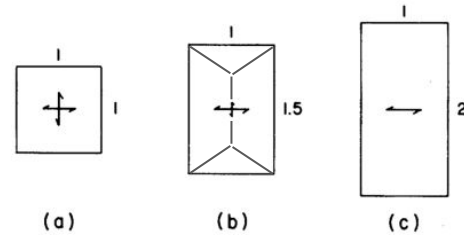
## Load Paths

### Floor Slabs

Concrete slabs span in the direction of the steel reinforcement.

**One-way slabs** should span the shortest direction.

**Two-way slabs** span in both directions. Aspect ratios should be square or less than 2:1. The load path divides at  $45^\circ$  from corner.



two-way slab tributary area of beam B

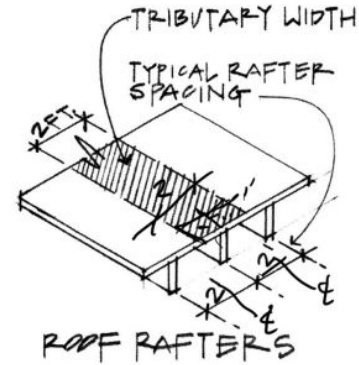


two-way waffle slab

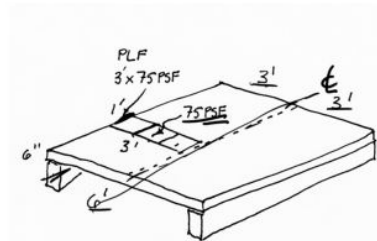
# Lecture: Load Tracing & Floor Systems (10/15)

## Tributary Area

The **tributary area** is an area used to determine the load on a member.



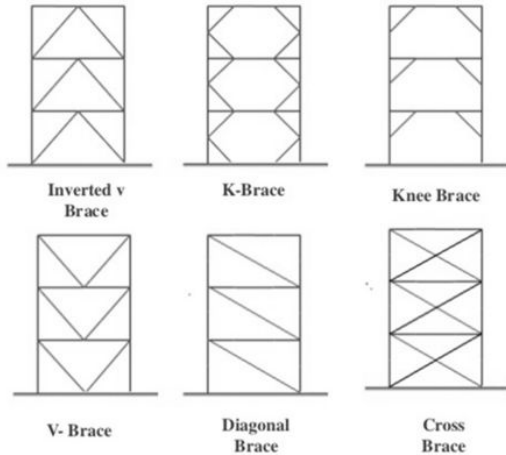
Each member has a tributary area that can be used to find the total load on that member.



# Lecture: Lateral Stability (10/20)

## Frame Bracing

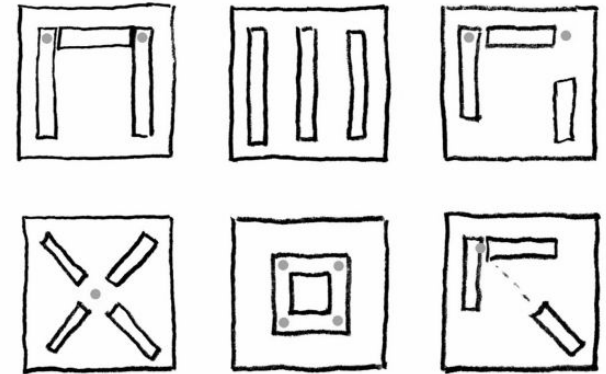
types of bracing



## Lateral Force Resistance

Stability requires at least 2 points of intersection.

Force is more evenly resisted with centroid of walls in the kern of slab



# Lecture: Stress and Strain (10/22)

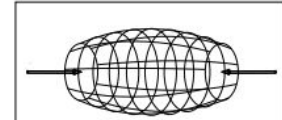
## Stress and Strain

- Stress
- Strain
- Analysis – ASD vs. LRFD
- Modes of Failure

## Types of Stress

- Compression

$$\sigma = \frac{P}{A}$$



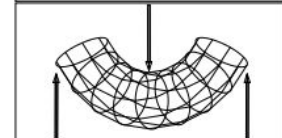
- Tension

$$\sigma = \frac{P}{A}$$



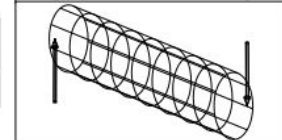
- Flexure

$$\sigma = \frac{M c}{I}$$



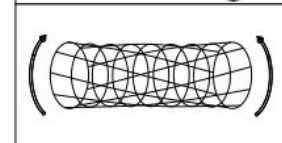
- Shear

$$\tau = \frac{P}{A} \text{ or } \frac{VQ}{Ib}$$



- Torsion

$$\tau = \frac{T r}{J}$$

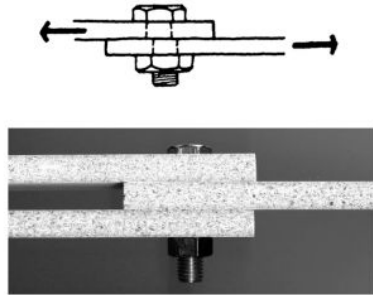


# Lecture: Stress and Strain (10/22)

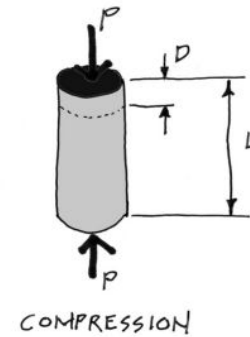
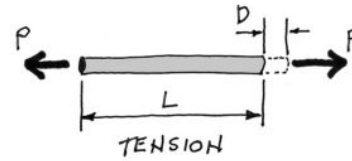
## Stress

Stress is the result of some force being applied to an area of some material.

$$\sigma = \frac{P}{A}$$



Shear Stress



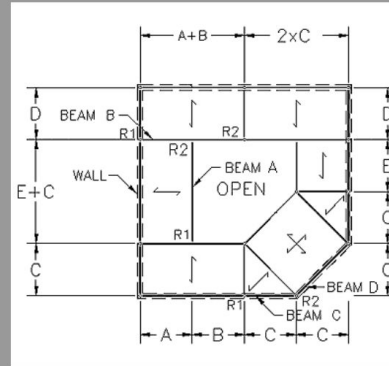
# HW #9: Floor Systems

## 9. Floor Systems

For each beam, A through G, determine the loading from the floor, the wall and from other beam reactions. Then, calculate the end reactions for each beam.

DATASET: 1

Span A	9 FT
Span B	11 FT
Span C	10 FT
Span D	14 FT
Span E	9 FT
Dead load of wall	255 PLF
Dead load of floor	21 PSF
Live load on floor	28 PSF

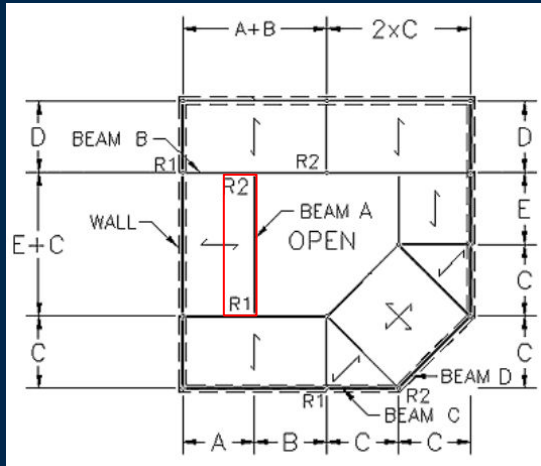


Your answer was correct.  
You scored 5 points.

#	Question	Your Response	Correct Answer	Score
1	Full uniform load on Beam A	220.5 PLF	220.5 PLF	5
2	End reaction R1 on Beam A	2094.75 LBS	2094.75 LBS	5
3	End reaction R2 on Beam A	2094.75 LBS	2094.75 LBS	5
4	Full uniform load on Beam B	343 PLF	343 PLF	5
5	Point load on Beam B	2094.75 LBS	2094.75 LBS	5
6	End reaction R1 on Beam B	4582.11 LBS	4582.11 LBS	5
7	End reaction R2 on Beam B	4372.64 LBS	4372.64 LBS	5
8	Full uniform load on Beam C	255 PLF	255 PLF	5
9	Peak value of triangular load on Beam C	122.5 PLF	122.5 PLF	5
10	End reaction R1 on Beam C	1683.35 LBS	1683.33 LBS	5
11	End reaction R2 on Beam C	1479.14 LBS	1479.17 LBS	5
12	Full uniform load on Beam D	255 PLF	255 PLF	5
13	Peak value of triangular load on Beam D	346.98 PLF	346.482 PLF	5
14	End reaction R1 on Beam D	3028.12 LBS	3028.12 LBS	5
15	End reaction R2 on Beam D	3028.12 LBS	3028.12 LBS	5

# HW #9: Floor Systems

DATASET: 1		-2-	-3-
Span A		9 FT	
Span B		11 FT	
Span C		10 FT	
Span D		14 FT	
Span E		9 FT	
Dead load of wall		255 PLF	
Dead load of floor		21 PSF	
Live load on floor		28 PSF	



Total uniform load of floor = dead load + live load

$$w = 21 \text{ PSF} + 28 \text{ PSF}$$

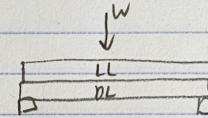
$$w = 49 \text{ PSF}$$

1. Full uniform load on beam A

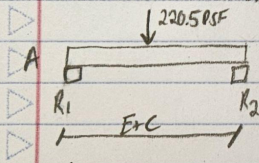
$$W_A = w \times \frac{A}{2}$$

$$= 49 \times \frac{9}{2}$$

$$W_A = 220.5 \text{ PLF}$$



2. End reactions on beam A



$$W_A = \text{uniform load} \times (E+C)$$

$$= 220.5 (9' + 10') = 4189.5 \text{ lbs}$$

$$\sum F_y = R_1 + R_2 - W_A$$

\* reactions are ~~equal~~ symmetrical \*

$$\sum F_y = 0 = 2R - 4189.5 \text{ lbs}$$

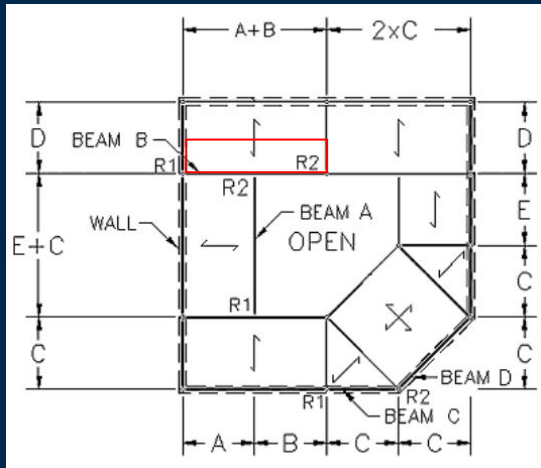
$$-2R = -4189.5 \text{ lbs}$$

$$R = 2094.75 \text{ lbs} \leftarrow \text{Answer to \#2 + \#3}$$

$\uparrow$   $R_1$  and  $R_2$

# HW #9: Floor Systems

DATASET: 1		-2-	-3-
Span A		9 FT	
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Span C		10 FT	
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Span E		9 FT	
Dead load of wall		255 PLF	
Dead load of floor		21 PSF	
Live load on floor		28 PSF	



4. Full uniform load on Beam B

$$w_B = w \times \frac{D}{2}$$

$$= 49 \times \frac{14}{2} = \boxed{343 \text{ PLF}}$$

5. Point load on Beam B

$$\text{point load} = R_2 \text{ of Beam A} = \boxed{2094.75 \text{ lbs}}$$

6. End reactions on Beam B

$$w_B = \text{uniform load} \times (A+B)$$

$$= 343 (9+11) = \underline{6860 \text{ lbs}}$$

$$\sum M_{R2A} = 0 = R_2A(A) + W_B \left( \frac{A+B}{2} \right) - R_2(A+B)$$

$$0 = 2094.75(9) + 6860 \left( \frac{9+11}{2} \right) - R_2(9+11)$$

$$20R_2 = \frac{18,1852.75 + 68,600}{20}$$

$$R_2 = \boxed{4372.64 \text{ lbs}} \leftarrow \text{Answer to \#7}$$

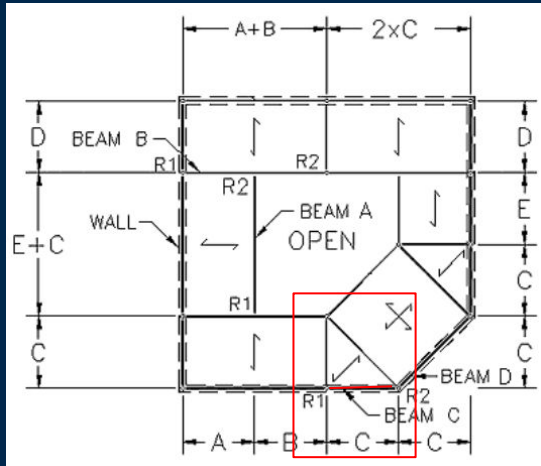
$$\sum F_y = 0 = -R_2A - W_B + R_2 + R_1$$

$$0 = -2094.75 - 6860 + 4372.64 + R_1$$

$$R_1 = \boxed{4582.11 \text{ lbs}} \leftarrow \text{Answer to \#6}$$

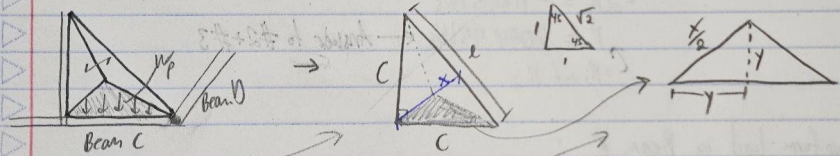
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Span C		10 FT	
Span D		14 FT	
Span E		9 FT	
Dead load of wall		255 PLF	
Dead load of floor		21 PSF	
Live load on floor		28 PSF	



8. Full uniform load on Beam C  
 = only one uniform load on Beam C  
 = dead load of wall - gives  
 = 1255 PLF

9. Peak value of triangular load on Beam C



$$d = \sqrt{c^2 + c^2} = c\sqrt{2}$$

$$x = \frac{1}{2}d = \frac{c\sqrt{2}}{4}$$

$$\sqrt{y^2 + y^2} = \frac{x}{2}$$

$$\sqrt{y^2 + y^2} = \frac{c\sqrt{2}}{4}$$

$$\left(\sqrt{y^2 + y^2} = \frac{c\sqrt{2}}{4}\right)^2$$

$$2y^2 = \frac{2c^2}{16}$$

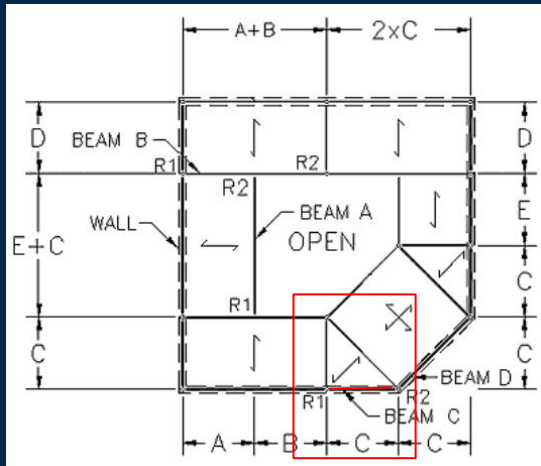
$$y^2 = \frac{c^2}{16}$$

$$y = \frac{c}{4}$$

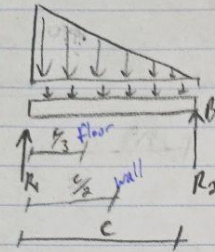
Peak floor load  
 = floor load  $\times \frac{c}{4}$   
 =  $419 \times \frac{10}{4}$   
 = 1047.5 PLF  
 Answer to #9

# HW #9: Floor Systems

DATASET: 1		-2-	-3-
Span A		9 FT	
Span B		11 FT	
Span C		10 FT	
Span D		14 FT	
Span E		9 FT	
Dead load of wall		255 PLF	
Dead load of floor		21 PSF	
Live load on floor		28 PSF	



10. End reactions



$$\begin{aligned} \text{floor load} &= \text{peak floor load} \times \frac{c}{2} \\ &= 122.5 \times \frac{10}{2} \\ &= 612.5 \text{ lbs} \end{aligned}$$

$$\begin{aligned} \text{wall load} &= \text{uniform Beam C load} \times c \\ &= 255 \times 10 \\ &= 2550 \text{ lbs} \end{aligned}$$

$$\begin{aligned} \sum M_{R_1} = 0 &= \text{floor} \left( \frac{c}{3} \right) + \text{wall} \left( \frac{c}{2} \right) - R_2 (c) \\ &= 612.5 \left( \frac{10}{3} \right) + 2550 \left( \frac{10}{2} \right) - 10R_2 \end{aligned}$$

$$10R_2 = 14,791.14$$

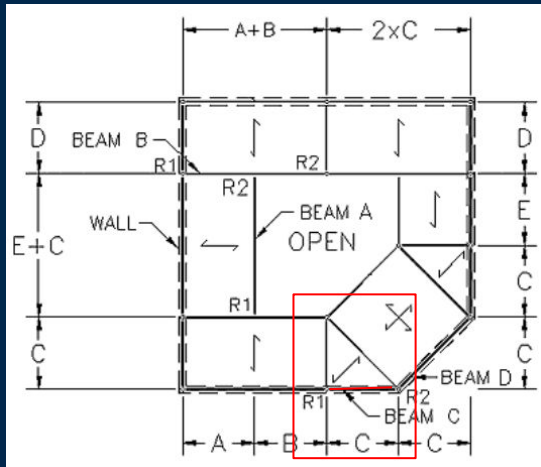
$$R_2 = 1,479.114 \text{ lbs} \leftarrow \text{Answer to \#11}$$

$$\begin{aligned} \sum F_y &= -\text{floor}_w - \text{wall}_w + R_1 + R_2 \\ &= -612.5 - 2550 + R_1 + 1479.14 \end{aligned}$$

$$R_1 = 1683.35 \text{ lbs} \leftarrow \text{Answer to \#10}$$

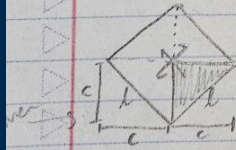
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12. Full uniform load on Beam D  
 = only one uniform load on Beam D  
 = dead load of wall - given  
 =  $\boxed{255 \text{ PLF}}$

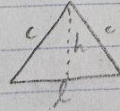
13. Peak value of triangular load on Beam D



$$l = c\sqrt{2} \text{ (from Beam C calc)}$$

$$= 10\sqrt{2} = \underline{14.14'}$$

$$h = \frac{1}{2}l = \frac{c\sqrt{2}}{2} = \frac{10\sqrt{2}}{2} = \underline{7.07'}$$

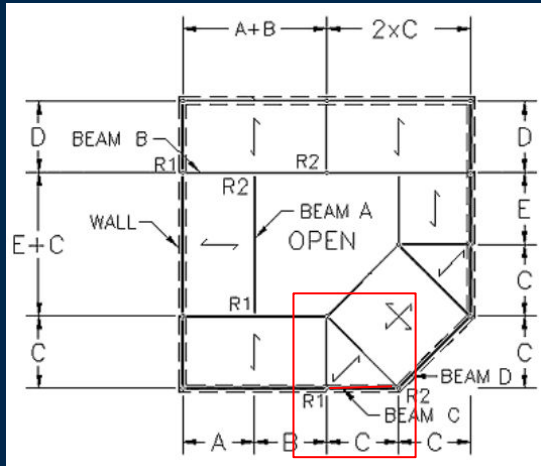


Peak value = height  $\times$  floor load

$$= 7.07' \times 49 = \boxed{346.98 \text{ PLF}} \leftarrow \text{Answer to \#13}$$

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14. End reactions on Beam D

$$\sum F_y = 0 = R_1 + R_2 - W_{\text{wall}} - \text{peak}$$

$$W_{\text{wall}} = w \times \sqrt{2} = 255 \times 10\sqrt{2} \quad \#12$$

$$= 3606.24$$

\* reactions are symmetrical \*

$$\text{Peak Floor} = \text{peak value} \times \frac{\sqrt{2}}{2} \quad \#10$$

$$= 2450$$

$$\sum F_y = 0 = 2R - W_{\text{wall}} - \text{peak floor}$$

$$= 2R - 3606.24 - 2450$$

$$2R = 6,056.24$$

$$R = \boxed{3028.12 \text{ lbs}} \leftarrow \text{Answer to \# 14 + 15}$$

$= R_1 \text{ and } R_2$

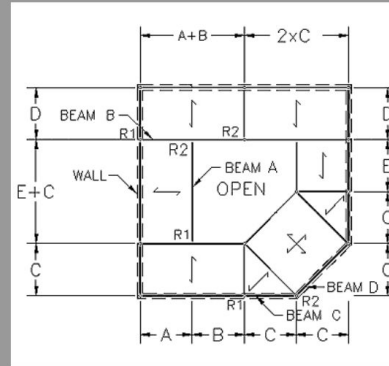
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LAB!